

Pre Calculus
Review 5.5 to 5.6

Name: Mr. Leckie
Block: _____

Calculator Allowed-SHOW ALL WORK FOR CREDIT

Find the area of each triangle.

1. $a = 5 \text{ cm}, b = 12 \text{ cm}, c = 13 \text{ cm}$

$$s = \frac{5+12+13}{2} = \frac{30}{2} = 15$$

$$A = \sqrt{15(15-5)(15-12)(15-13)}$$

$$\boxed{A \approx 30 \text{ cm}^2}$$

2. $c = 3.58 \text{ m}, b = 6.8 \text{ m}, A = 39^\circ$

$$A = \frac{1}{2} bc \sin A$$

$$A = \frac{1}{2} (6.8)(3.58) \sin(39^\circ)$$

$$\boxed{A \approx 7.660 \text{ m}^2}$$

Solve each triangle. If there is no solution, explain why. If there are two triangles, solve BOTH!

3. $b = 40, c = 45, A = 51^\circ$



(SAS) → (1Δ)

$$a^2 = 40^2 + 45^2 - 2(40)(45) \cos(51^\circ)$$

$$\boxed{a \approx 36.871}$$

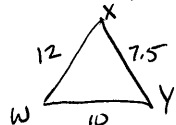
$$40^2 = a^2 + 45^2 - 2a(45) \cos B$$

$$\cos^{-1}\left(\frac{40^2 - a^2 - 45^2}{-2a(45)}\right) = B$$

$$\boxed{57.469^\circ \approx B}$$

$$\boxed{71.531^\circ \approx C}$$

5. $w = 7.5, x = 10, y = 12$



(SSS) → (1Δ)

$$12^2 = 10^2 + 7.5^2 - 2(10)(7.5) \cos Y$$

$$\cos^{-1}\left(\frac{12^2 - 10^2 - 7.5^2}{-2(10)(7.5)}\right) = Y$$

$$\boxed{85.316^\circ \approx Y}$$

$$10^2 = 7.5^2 + 12^2 - 2(7.5)(12) \cos X$$

$$\cos^{-1}\left(\frac{10^2 - 7.5^2 - 12^2}{-2(7.5)(12)}\right) = X$$

$$\boxed{56.155^\circ \approx X} \Rightarrow \boxed{W \approx 38.529^\circ}$$

4. $c = 125, b = 150, C = 25^\circ$

$$\frac{\sin 25^\circ}{125} = \frac{\sin B}{150}$$

$$B = \sin^{-1}\left(\frac{150 \sin(25^\circ)}{125}\right)$$

$$\boxed{B_1 \approx 30.474^\circ}$$

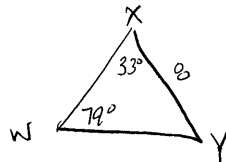
$$\boxed{A_1 \approx 124.526^\circ}$$

$$\frac{\sin 25^\circ}{125} = \frac{\sin A_1}{a_1}$$

$$a = \frac{125 \sin A}{\sin 25^\circ}$$

$$\boxed{a \approx 243.679}$$

6. $w = 8, W = 79^\circ, X = 33^\circ$



(AAS) → (1Δ)

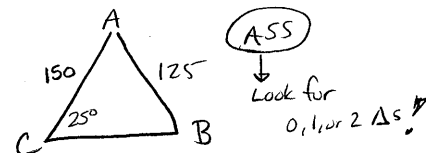
$$\boxed{XY = 68^\circ}$$

$$\frac{\sin 79^\circ}{8} = \frac{\sin 33^\circ}{x}$$

$$\boxed{x = \frac{8 \sin(33^\circ)}{\sin(79^\circ)} \approx 4.439}$$

$$\frac{\sin 79^\circ}{8} = \frac{\sin 68^\circ}{y}$$

$$\boxed{y = \frac{8 \sin(68^\circ)}{\sin(79^\circ)} \approx 7.556}$$



$$\rightarrow \text{or} \rightarrow 180 - B_1 = B_2$$

$$\boxed{149.526^\circ = B_2}$$

$$\boxed{5.474^\circ \approx A_2}$$

$$\frac{\sin A_2}{a_2} = \frac{\sin 25^\circ}{125}$$

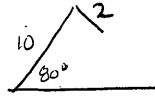
$$a_2 = \frac{125 \sin(A_2)}{\sin 25^\circ}$$

$$\boxed{a_2 \approx 28.213}$$

7. Given an example where three parts of a triangle are given, but no triangle can be formed. Explain your answer including a diagram.

Option #1 ... ASS

where the 2nd side is too short



Option #2 ... SSS where the sum of the 2 smallest sides is smaller than the 3rd side

(ex) $a = 10, b = 12, c = 25$

For questions 8-9, do NOT copy a question on any of the worksheets for 5.5 or 5.6!! **Make your own problem!!** you may choose whether or not a diagram is given in the problem.

8. Create a new application question that whose solution is found using the Law of Sines. Then, solve your problem.

SHARE
w/ SOMEONE
ELSE FOR
PRACTICE!

9. Create a new application question that whose solution is found using the Law of Cosines. Then, solve your problem.