

Pre Calculus
Chapter 2B Review

Name: KEY
Block: _____

No Calculator. Show all applicable work for full credit.

For 1-3, simplify each expression. Write answers in $a + bi$ form.

1. $\sqrt{-36}$

$$\boxed{6i}$$

2. $(3+4i) - (2-6i)$

$$3+4i - 2+6i$$

$$\boxed{1+10i}$$

$$3. \frac{(4+2i)(5+i)}{(5-i)(5+i)} = \frac{20+4i+10i+2i^2}{25+5i-5i-i^2} \\ = \frac{20+14i-2}{25+1}$$

In question 4-5, solve.

4. $x^2 - 6x + 10 = 0$

$$x = \frac{6 \pm \sqrt{36-4(1)(10)}}{2(1)} = \frac{6 \pm \sqrt{-4}}{2}$$

$$= \frac{6 \pm 2i}{2} = \boxed{3 \pm i}$$

5. $4x^2 = 8x - 5$

$$4x^2 - 8x + 5 = 0$$

$$x = \frac{8 \pm \sqrt{64-4(4)(5)}}{2(4)} = \frac{8 \pm \sqrt{-16}}{8} = \frac{8 \pm 4i}{8}$$

$$= \frac{18+14i}{26} = \boxed{\frac{9}{13} + \frac{7}{13}i}$$

Write the polynomial, in standard form, whose zeros include those listed below.

$$\boxed{1 \pm \frac{1}{2}i}$$

6. -3 (multiplicity 2) and 5

$$(x+3)^2(x-5)$$

$$(x^2+6x+9)(x-5)$$

$$x^3 - 5x^2 + 6x^2 - 30x + 9x - 45$$

$$\boxed{x^3 + x^2 - 21x - 45}$$

7. 2 and $1+2i$

$$(x-2)[x - (1+2i)][x - (1-2i)]$$

$$(x-2)(x-1-2i)(x-1+2i)$$

$$(x-2)(x^2 - x + 2ix - x + 1 - 2i - 2ix + 2i - 4i^2)$$

$$(x-2)(x^2 - 2x + 1 + 4)$$

$$(x-2)(x^2 - 2x + 5)$$

$$x^3 - 2x^2 + 5x - 2x^2 + 4x - 10 = \boxed{x^3 - 4x^2 + 9x - 10}$$

8. Using the given zero, find all the zeros and write the function as the product of linear and irreducible quadratic factors.

$1-3i$ is a zero of $2x^4 - 15x^3 + 36x^2 - 98x - 60$; $1+3i$ is also a zero

$$(1-3i)(-13-6i) = -13-6i+39i+\frac{-18}{+18i^2} = -31+33i$$

$$(1-3i)(5+33i) = 5+33i-15i-\frac{-99i^2}{+99i^2} = 104+18i$$

$$(1-3i)(6+18i) = 6+18i-18i-\frac{-54i^2}{+54i^2} = 60$$

$$\begin{array}{r} 1-3i \boxed{2} -15 \quad 36 \quad -98 \quad -60 \\ \underline{-6i} \quad -31+33i \quad 104+18i \quad 60 \\ \hline 1+3i \boxed{2} -13-6i \quad 5+33i \quad 6+18i \quad 0 \\ \underline{+6i} \quad -11-33i \quad -6-18i \\ \hline 2 \quad -11 \quad -6 \quad 0 \end{array}$$

$$2x^2 - 11x - 6 = 0$$

$$(2x+1)(x-6) = 0$$

$$2x+1=0 \quad x-6=0$$

$$x = -\frac{1}{2} \quad x = 6$$

$$= [x - (1-3i)][x - (1+3i)]$$

$$= (x-1+3i)(x-1-3i)$$

$$= x^2 - 2x + 1 + 9 = x^2 - 2x + 10$$

ZEROS

$$x = 1-3i$$

$$x = 1+3i$$

$$x = -\frac{1}{2}$$

$$x = 6$$

FACTORS (Linear & Irreducible Quadratic)

$$(2x+1)(x-6)(x^2 - 2x + 10)$$

For questions 9-11, determine (if it exists):

- a) end behavior including HA or Slant Asymp.
- b) vertical asymptotes
- c) x-intercept(s)

d) y-intercept

e) graph (with enough points to be accurate)

9. $y = \frac{2x+3}{x-1}$

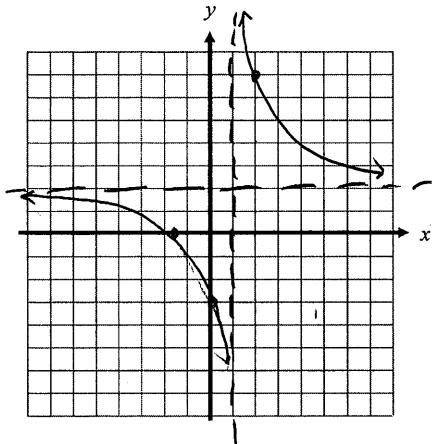
a) HA: $y = 2$

b) VA: $x = 1$

c) x-int: $(-\frac{3}{2}, 0)$
 $0 = 2x+3$
 $-\frac{3}{2} = x$

d) y-int: $(0, -3)$

$$\begin{array}{r} x \\ 2 \\ \hline 1 \\ 4 \\ \hline 3 \\ \hline \end{array} \quad \frac{4+3}{2-1} = 7$$



10. $y = \frac{x^2 - 2x - 8}{x - 4} = \frac{(x-4)(x+2)}{x-4} = x+2$

a) NO HA

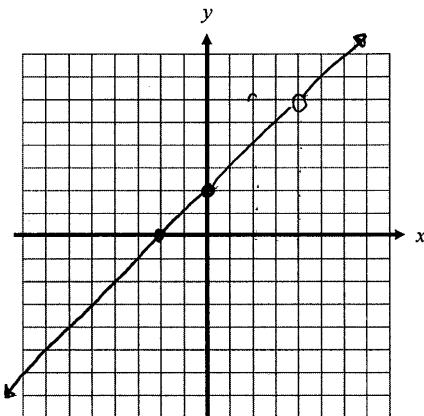
b) NO VA $\frac{\text{HOLE}}{\downarrow} @ x=4$
 $\uparrow (4, 6)$

c) x-int: $(-2, 0)$

$$0 = \frac{x+2}{x}$$

d) y-int: $(0, 2)$

:

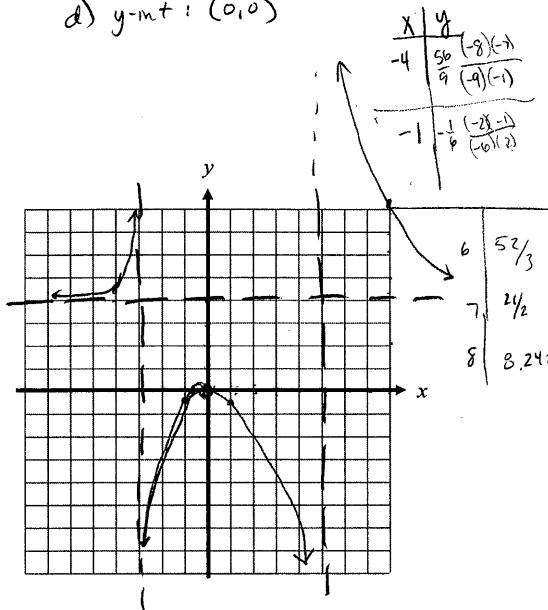


a) HA: $y = 4$

b) VA: $x = 5$ and $x = -3$

c) x-int: $(0, 0)$ and $(-1/2, 0)$

d) y-int: $(0, 0)$



12. Identify the x values that cause the function to be zero, positive, negative and undefined.

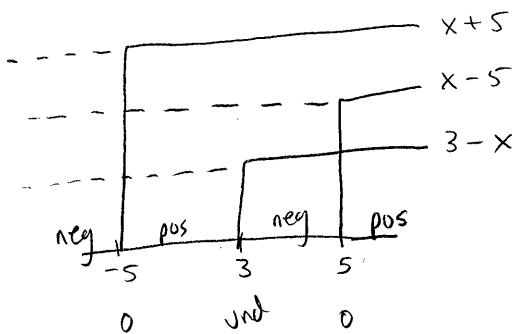
$$f(x) = \frac{x^2 - 25}{3-x} = \frac{(x+5)(x-5)}{3-x}$$

$f(x) = 0$ at $x = -5$ and $x = 5$

$f(x) > 0$ on $(-5, 3) \cup (5, \infty)$

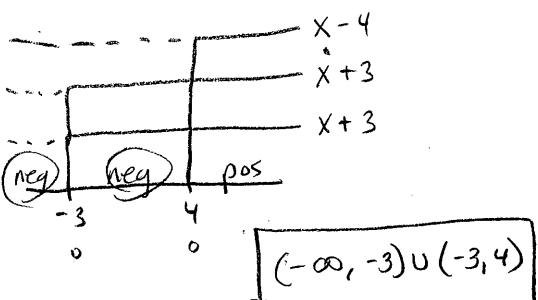
$f(x) < 0$ on $(-\infty, -5) \cup (3, 5)$

$f(x)$ is undefined at $x = 3$



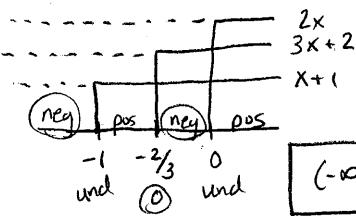
Solve the inequality using a sign chart.

13. $(x-4)(x+3)^2 < 0$ neg



14. $\frac{3x+2}{2x^2+2x} \leq 0$

$\frac{3x+2}{2x(x+1)} \leq 0$ neg or 0

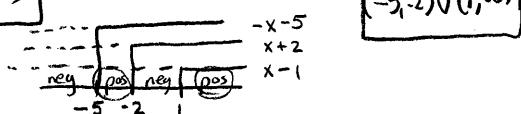


15. $\frac{1}{x+2} - \frac{2}{x-1} > 0$

$\frac{1}{(x+2)(x-1)} - \frac{2}{(x-1)(x+2)} > 0$

$\frac{x-1-2x-4}{(x+2)(x-1)} > 0$

$\frac{-x-5}{(x+2)(x-1)} > 0$ pos



Calculator Allowed. Show all applicable work for full credit.

16. Find and verify all the zeros and write the function as the product of linear and irreducible quadratic factors.

a) $f(x) = x^4 - 8x^3 + 33x^2 - 68x + 52$

Graph $f(x)$... $x=2$ looks like a zero w/multiplicity 2

$$\begin{array}{r} 2 | 1 & -8 & 33 & -68 & 52 \\ & 2 & -12 & 42 & -52 \\ \hline 2 | 1 & -6 & 21 & -26 & 0 \\ & 2 & -8 & 26 & \\ \hline & 1 & -4 & 13 & 0 \end{array}$$

$$x^2 - 4x + 13 = 0$$

$$x^2 - 4x + 4 = -13 + 4$$

$$(x-2)^2 = -9$$

$$x-2 = \pm 3i$$

$$x = 2 \pm 3i$$

b) $f(x) = 6x^4 - 7x^3 - x^2 + 67x - 105$

graph $f(x)$... $x = 3/2$

$$\begin{array}{r} 3/2 | 6 & -7 & -1 & 67 & -105 \\ & 9 & 3 & 3 & 105 \\ \hline -7/3 | 6 & 2 & 2 & 70 & 0 \\ & -14 & 28 & -70 & \\ \hline & 6 & -12 & 30 & 0 \end{array}$$

$$6x^2 - 12x + 30 = 0$$

$$6(x^2 - 2x + 5) = 0$$

$$x^2 - 2x + 5 = 0$$

$$x = \frac{2 \pm \sqrt{4-4(1)(5)}}{2(1)} = \frac{2 \pm \sqrt{-16}}{2} = \frac{2 \pm 4i}{2}$$

$$= 1 \pm 2i$$

ZEROS
 $x=2$ mult = 2
 $x=2+3i$
 $x=2-3i$

FACTORS (Linear & Irreducible Quadratic Factors)
 $f(x) = (x-2)^2 (x^2 - 4x + 13)$

ZEROS:
 $x = 3/2$
 $x = -7/3$
 $x = 1+2i$
 $x = 1-2i$

17. Solve graphically: $2x^3 - 5x^2 + 3x \leq 0$

FACTORS
 $(x - 3/2)(x + 7/3)(6x^2 - 12x + 30)$