

**Honors Algebra 2**  
**Chapter 3 Review**

**Name:** \_\_\_\_\_  
**Block:** \_\_\_\_\_

**NON-CALCULATOR**

3-1 In 1-2, determine if the following is a polynomial or not. If it is, put it in standard form and give the degree. If it is not, explain why not.

1)  $-5x^2 - 7x^5 + 8 + 3x^4$

2)  $15x + 4\sqrt{x^3} - x^5$

3:1-2 In 3-5, perform the indicated operation.

3)  $(3x^3 + 2x^2 - 4x + 1) + (-6x^3 + 11x + 6)$

4)  $(8 - 6x^2 + x^3 - x + 7x^4) - (3 - 5x^3 + 2x + 4x^4)$

5)  $(-4x^3 + 2x - 9)(5x^2 - 3x + 7)$

3-3 6) Divide using long division:  $\frac{9x^3 - 4x + 5}{3x - 1}$

3-3 Use synthetic substitution to evaluate the given polynomial for  $x = -2$

7)  $6x^4 - 3x^3 - 12x^2 - 5x + 6$

8)  $x^4 - 3x^3 - 11x^2 - 9$

3-4 9) Factor each expression

a)  $27x^6 + 125$

b)  $y^3 + 7y^2 + 2y + 14$

c)  $6x^4 - 23x^2 + 20$

3-5 10) Determine all the solutions of  $f(x) = 4x^3 + 12x^2 - x - 3$  by factoring.

3:4-6 Find all real and imaginary zeros of each function.

11)  $f(x) = (2x - 3)(4 - x)(x + 7)$

12)  $f(x) = 2x^3 + x^2 - 13x + 6$ ; given -3 is a zero

13)  $f(x) = 5x^4 + 3x^3 + 3x^2 + 3x - 2$ ; given -1 and  $\frac{2}{5}$  are zeros.

3-6 14). Write the simplest polynomial function in factored form with the given zeros.

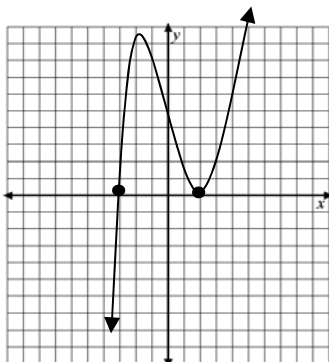
a) zeros of  $-\frac{6}{5}$  and 2 (multiplicity of 2)

b) zeros of 3 and  $\sqrt{2}$

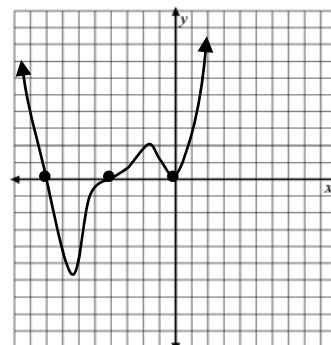
c) zeros of 5 and  $-3i$

3-7 For the graphs below, identify whether the function has an even or odd degree and positive or negative leading coefficient. Also, identify the zeros and their multiplicity.

15)



16)



3:6-7 17) Can a 5<sup>th</sup> degree polynomial...

a) have 4 turning points? Explain.

b) have 6 zeros? Explain.

c) have exactly 2 real zeros of multiplicity 1? Explain.

3-7 For questions 18-19, find each of the following for the given function:

a) List the degree.

b) Describe the end behavior using infinity notation.

c) Find the zeros (including their multiplicity).

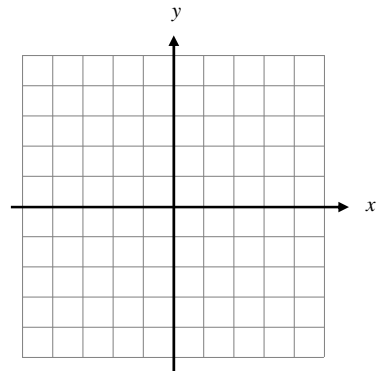
d) Based on the information from parts (a) through (c), sketch a graph of the function. Your sketch should have a scale on the  $x$ -axis only.

18)  $f(x) = -2x(x+3)(x-4)^2$

19)  $f(x) = x^3 + 3x^2 - 9x - 27$

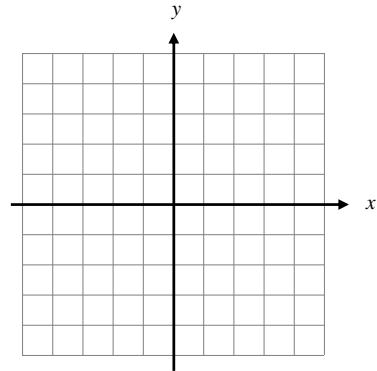
3-8 20) Consider the parent function  $f(x) = x^3$ . Rewrite given the following transformations and then sketch the transformed graph:

Vertical Stretch by a factor of 3 followed by a horizontal translation 2 units right and a vertical translation 2 units up.



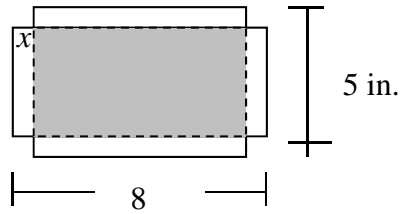
- 3-8 21) Consider the parent function  $f(x) = x^4$ . Rewrite given the following transformations and then sketch the transformed graph:

Reflection across the  $x$ -axis followed by a horizontal compression by a factor of  $\frac{1}{4}$ .



**CALCULATOR ALLOWED**

- 3-2 22) You are making an open box to hold paper clips out of a piece of cardboard that is 5 inches by 8 inches. The box will be formed by making an  $x$  inch by  $x$  inch square cut out of the corners as shown in the diagram and folding up the sides. **You want the box to have the greatest volume possible.**



- Write an equation for the Volume of the box as a function of the length of the cut,  $x$ .
- Use a graphing calculator to find how long you should make the cuts. Explain your reasoning.
- What is the maximum volume of the box?
- What will the dimensions of the finished box be?

3-7 Graph the polynomial to find all local minimum(s) and maximum(s). Then give the domain and range.

23)  $f(x) = 2x^6 + 10x^3 - 7x + 3$

24)  $f(x) = -x^5 + 6x^3 - 5x - 3$

3-9 25) Find and **verify** all zeros of the function. **SHOW ALL WORK!!!**

$$y = 2x^3 + 3x^2 - 3x + 5$$

3-9 26) The table shows the number of sandwiches sold each day at a deli over 5 days.

|            |     |    |    |     |    |    |
|------------|-----|----|----|-----|----|----|
| Day        | 0   | 1  | 2  | 3   | 4  | 5  |
| Sandwiches | 196 | 57 | 72 | 101 | 89 | 66 |

a) Determine the degree of the polynomial that would fit the data. Explain how you know.

b) Write a polynomial function for the data.

c) Use your function from part b to determine the number of sandwiches expected to be sold on day 6.

**REMEMBER:** Any questions from the previous chapter reviews are fair game for this test!!!