

Algebra 1B

Chapter 7 Review: Linear Systems

Name KEY
Block _____ Date _____

Calculator NOT Allowed

1. Is (2, 5) a solution of the following system? Explain.

$$y = 2x + 1$$

$$2x - y = 8$$

Plug in $x=2$ & $y=5$ to both...

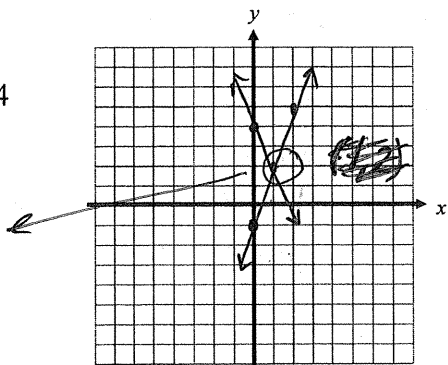
$$\begin{aligned} 5 &= 2(2) + 1 \\ &= 4 + 1 \\ &= 5 \checkmark \end{aligned}$$

$$\begin{aligned} 2(2) - (5) &= 8 \\ 4 - 5 &\neq 8 \quad \times \end{aligned}$$

NO since (2,5)
Didn't work for BOTH!

Solve each system by graphing.

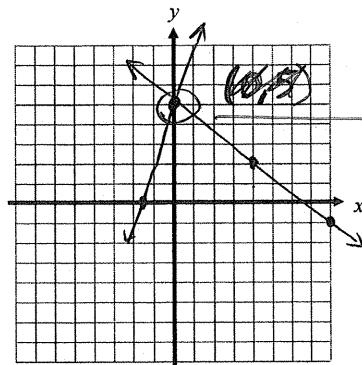
2. $y = 3x - 1$
 $y = -2x + 4$



(1, 2)

3. $y = -\frac{3}{4}x + 5$
 $10x - 3y = -15$

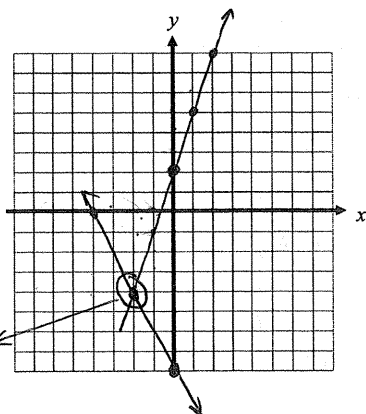
$$\begin{array}{r|l} x & y \\ \hline 0 & 5 \\ -3 & -15 \\ \hline -3 & -15 \\ \hline 1 & 5 \end{array}$$



(0, 5)

4. $y = 3x + 2$
 $2x + y = -8$

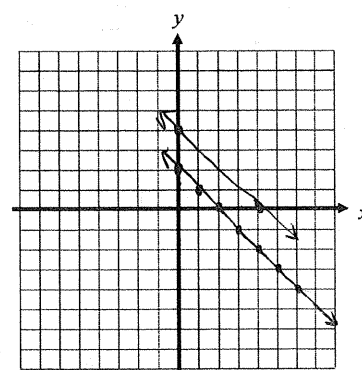
$$\begin{array}{r|l} x & y \\ \hline 0 & -8 \\ -4 & 0 \end{array}$$



(-2, -4)

5. $y = -x + 2$
 $3x + 3y = 12$

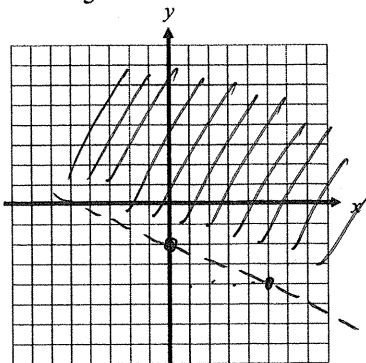
$$\begin{array}{r|l} x & y \\ \hline 0 & 4 \\ 4 & 0 \end{array}$$



Parallel Lines
NO SOLUTION

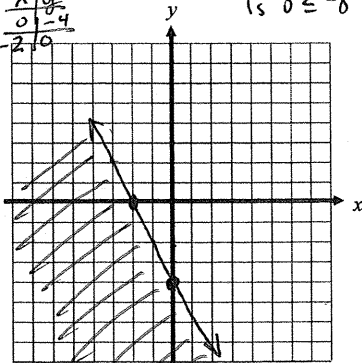
Graph each inequality.

6. $y > -\frac{2}{5}x - 2$



7. $4x + 2y \leq -8$

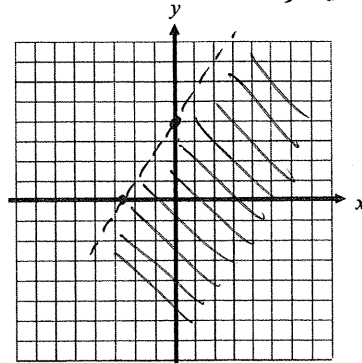
$$\begin{array}{r|l} x & y \\ \hline 0 & -4 \\ -2 & 0 \end{array}$$



TEST (0,0)
Is $0 \leq -8$? No!

8. $6x - 4y > -16$

$$\begin{array}{r|l} x & y \\ \hline 0 & 4 \\ -8 & 0 \end{array}$$



TEST (0,0)
Is $0 > -16$? Yes

Graphing Calculator Allowed

Solve each system using substitution. ★★

9. $x = y - 7$
 $2x + y = -8$

$x = 2 - 7 = -5$

$(-5, 2)$

Ans
 $2(y - 7) + y = -8$
 $2y - 14 + y = -8$
 $3y - 14 = -8$
 $3y = 6 \Rightarrow y = 2$

10. $y = 3x - 10$
 $y = 8x + 5$

$3x - 10 = 8x + 5$
 $-15 = 5x$
 $-3 = x$
 $y = 3(-3) - 10 = -9 - 10 = -19$

$(-3, -19)$

11. $2x + 4y = -6$
 $x - 3y = 7 \rightarrow x = 7 + 3y$

$2(7 + 3y) + 4y = -6$
 $14 + 6y + 4y = -6$
 $10y = -20$
 $y = -2$

$x = 7 + 3(-2)$
 $x = 7 - 6$
 $x = 1$

$(1, -2)$

12. $4x + y = -2 \rightarrow y = -2 - 4x$
 $-2x - 3y = 1$

$-2x - 3(-2 - 4x) = 1$
 $-2x + 6 + 12x = 1$
 $10x = -5$
 $x = -1/2$

$y = -2 - 4(-1/2)$
 $y = -2 + 2$
 $y = 0$

$(-1/2, 0)$

Solve each system using elimination.

13. $x + 2y = 7$
 $3x - 2y = -3$

$4x = 4$
 $x = 1$

(1) $+2y = 7$
 $2y = 6$
 $y = 3$

$(1, 3)$

14. $9x - 3y = 24$
 $7x - 3y = 20$

$2x = 4$
 $x = 2$

$9(2) - 3y = 24$
 $18 - 3y = 24$
 $-3y = 6$
 $y = -2$

$(2, -2)$

15. $-6x + 12y = 96$
 $2(3x - 6y = -48) \Rightarrow$

$-6x + 12y = 96$
 $6x - 12y = -96$
 $0 = 0$ TRUE!

∞ Solutions

16. $-3(4x - 3y = 11) \Rightarrow$
 $4(3x - 5y = -11)$

$-12x + 9y = -33$
 $12x - 20y = -44$
 $-11y = -77$
 $y = 7$

$4x - 3(7) = 11$
 $4x - 21 = 11$
 $4x = 32$
 $x = 8$

$(8, 7)$

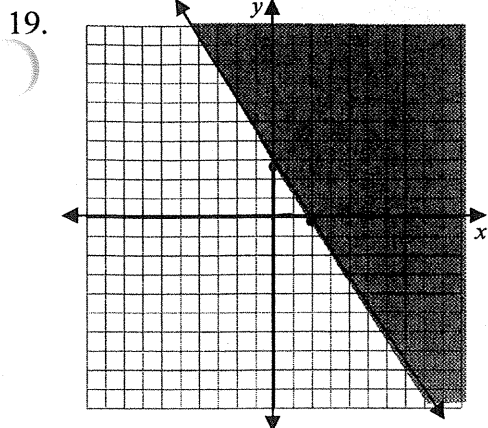
Solve each system by graphing using your graphing calculator. ** ... not required in this chapter **

17. $y = x - 5$
 $y = 2x + 1$

Press Y= ... (as long as the equation is solved for y)
 Enter first equation as Y1 and second equation as Y2
 2nd TRACE (Calc) ... 5 ... Enter,
 Enter, Enter

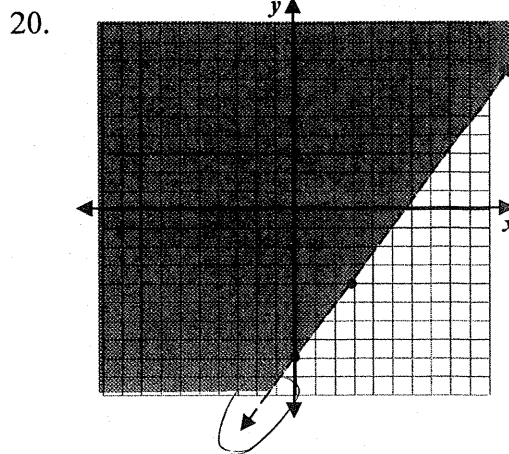
18. $x + y = -10$
 $2x + 3y = -30$

Write the linear inequality shown on the graph.



y -intercept = 3
 slope = $-\frac{3}{2}$
 SHADED ABOVE & SOLID LINE

$y \geq -\frac{3}{2}x + 3$

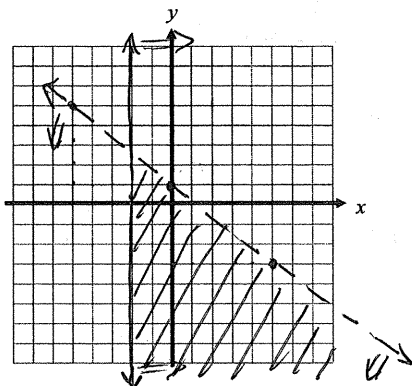


y -int: -8
 slope = $\frac{4}{3}$
 Dashed Line
 SHADDED ABOVE

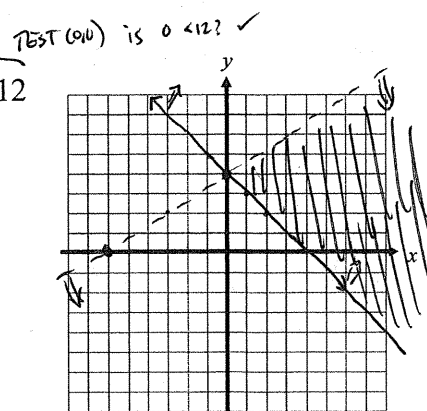
$y > \frac{4}{3}x - 8$

Graph each system of inequalities.

21. $x \geq -2$
 $y < -\frac{4}{5}x + 1$



22. $-2x + 3y < 12$
 $y \geq -x + 4$



Use a system of equations to solve each word problem.

23. Suppose your community center sells a total of 292 tickets for a basketball game. An adult ticket costs \$3. A student ticket costs \$1. The sponsors collect \$470 in ticket sales. Write and solve a system of linear equations to find the number of each type of ticket sold.

a = # of adult tickets
 k = # of student tickets

$a + k = 292$
 $3a + 1k = 470$

89 adult tickets
 203 student tickets

Solve by elimination... (subtract)

$-2a = -178$

$a = 89$

24. Suppose you bought supplies for a party. Three rolls of streamers and 15 party hats cost \$30. Later, you bought 2 rolls of streamers and 4 party hats for \$11. Write and solve a system of linear equations to find the cost of each roll of streamers and each party hat.

r = cost of a roll of streamers
 h = cost of a party hat

$\left. \begin{matrix} 3r + 15h = 30 \\ 2r + 4h = 11 \end{matrix} \right\} \begin{matrix} -2 \\ 3 \end{matrix}$

Solve by elimination

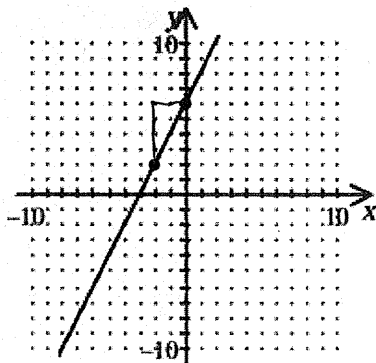
$\Rightarrow \begin{matrix} -6r - 30h = -60 \\ 6r + 12h = 33 \\ \hline -18h = -27 \\ h = 1.5 \end{matrix}$

$2r + 4(1.5) = 11$
 $2r + 6 = 11$
 $2r = 5$
 $r = \frac{5}{2}$

\$1.50 for a party hat
 \$2.50 for a roll of streamers

Previous Chapter Review

25. Find the slope of the line.



Rise = 4

Run = 2

Slope = $\frac{4}{2}$

26. Suppose the following two points are on a line: $(-4, 10)$ and $(6, 5)$

a) Find the slope $\frac{y_2 - y_1}{x_2 - x_1} = \frac{10 - 5}{-4 - 6} = \frac{5}{-10} = \boxed{-\frac{1}{2}}$

b) Write the equation of the line in point-slope form.

$(-4, 10)$: $y - 10 = -\frac{1}{2}(x + 4)$

OR

$(6, 5)$: $y - 5 = -\frac{1}{2}(x - 6)$

c) Write the equation of the line in slope-intercept form.

$y - 10 = -\frac{1}{2}x - 2$

$y = -\frac{1}{2}x + 8$

~~$y - 5 = -\frac{1}{2}x + 3$~~

$y - 5 = -\frac{1}{2}x + 3$

$y = -\frac{1}{2}x + 8$

SAME ANSWER!

d) Write the equation of the line in standard form.

$[y = -\frac{1}{2}x + 8] \cdot 2$

$2y = -x + 16$

$x + 2y = 16$